

# Modeling of Sub Threshold Current and Sub Threshold Swing of Short-Channel Fully-Depleted SOI MOSFET with Back-Gate Control

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## Abstract

*The present paper deals with the analytical modeling of subthreshold characteristics of short-channel fully-depleted recessed-source/drain SOI MOSFET with back-gate control. The variations in the subthreshold current and subthreshold swing have been analyzed against the back-gate bias voltage, buried-oxide (BOX) thickness and recessed source/drain thickness to assess the severity of short-channel effects in the device. The model results are validated by simulation data obtained from two-dimensional device simulator ATLAS from Silvaco.*

## 1. INTRODUCTION

It has been known that the short-channel effects are well suppressed in a FD SOI MOSFET, when the silicon channel thickness ( $t_{Si}$ ) is less than or equal to one-fourth of the channel length ( $L$ ). However, in sub 30 nm channel length regime,  $t_{Si}$  needs to be scaled below 5nm; therefore, the large parasitic series resistance and threshold voltage sensitivity to  $t_{Si}$  variation become serious issues [1, 2]. The extended source and drain offer low source and drain resistance, respectively, and facilitate better source and drain contacts and consequently decrease the total series resistance [3]. The presence of a back-gate in FD Re-S/D SOI MOSFETs could be a potential option to improve the device performance in terms of less parasitic series resistance, on-current ( $I_{on}$ ) improvement, and off-current ( $I_{off}$ ) suppression as well [4]. Keeping in view the above facts, an attempt has been made

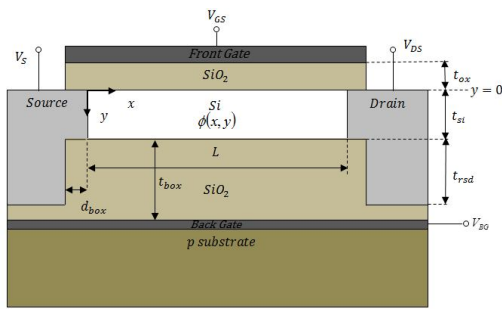
in this paper to present a theoretical and simulation-based study of subthreshold swing and subthreshold current of the FD Re-S/D SOI MOSFETs with back-gate control.

## 2. DEVICE STRUCTURE

The schematic structure of a Re-S/D UTB SOI MOSFET with back-gate control is shown in Fig.1, where,  $L$  is the gate length,  $t_{Si}$  is the Si film thickness,  $t_{ox}$  is the gate oxide thickness and  $t_{box}$  is the buried oxide thickness.  $N_a$ ,  $N_d$  and  $N_{sub}$  represent channel, source/drain, and substrate doping concentrations respectively.  $V_{Gs}$ ,  $V_{DS}$  and  $V_{BG}$  are the gate to source, drain to source, and back-gate voltages, respectively. The symbols of work functions of front- and back-gate materials are taken to be  $\phi_{FM}$  and  $\phi_{BM}$  respectively.

In the present structure, since we have considered a separate back gate on the substrate as done in Ref. [5], the substrate doping really does

not matter much and the substrate only provide mechanical support to the structure. The doping density in the channel region is considered to be uniform and the influence of charge carriers and fixed oxide charge on the electrostatics of the channel is neglected. The x- and y-axes of the 2D structure are considered to be along the channel-gate oxide interface and the source-channel interface respectively, as shown in Fig.1.



**Fig.1:** The Schematic Structure of the Re-S/D FD SOI MOSFET with Back-Gate control

The other parameters used in modeling and simulation are detailed in Table 1.

**Table-1:** Device Dimensions and Parameters used for Modeling and Simulation

Parameters	Symbol	Values
Front-gate work-function	$\phi_{FM}$	4.71 eV, 4.8 eV
Back-gate work-function	$\phi_{BM}$	4.71 eV, 4.8 eV
Channel Doping	$N_a$	$10^{15} \text{ cm}^{-3}$
Source/Drain Doping	$N_d$	$10^{20} \text{ cm}^{-3}$
Substrate Doping	$N_{sub}$	$10^{15}$
Silicon Thickness	$t_{Si}$	6-10 nm
Gate Oxide Thickness	$t_{ox}$	1.5-3 nm
Buried Oxide Thickness	$t_{box}$	40-80 nm
The depth of S/D in the buried oxide	$t_{rsd}$	0- 25 nm
Recessed Length	$d_{box}$	3 nm
Channel Length	$L$	20-120 nm
Gate-to-Source Voltage	$V_{GS}$	-0.2 V to 0.6 V
Drain Voltage	$V_{DS}$	0.05 V
Back-gate Voltage	$V_{BG}$	-5 to 2 V

### 3. THEORETICAL MODELING

The two-dimensional channel potential  $\phi(x, y)$  can be obtained by solving the following 2D Poisson's equation

$$\frac{\partial^2 \phi(x, y)}{\partial x^2} + \frac{\partial^2 \phi(x, y)}{\partial y^2} = \frac{qN_a}{\epsilon_{Si}} ;$$

$$0 \leq x \leq L, 0 \leq y \leq t_{Si} \quad (1)$$

The potential profile in the vertical direction (y-dependence of  $\phi(x, y)$ ) in the channel can be approximated by following parabolic function [6].

$$\phi(x, y) = \phi_f(x) + C_1(x)y + C_2(x)y^2 \quad (2)$$

where,  $\phi_f(x) = \phi(x, 0)$  is the surface potential at SiO<sub>2</sub>/Si interface and the arbitrary coefficients  $C_1(x)$  and  $C_2(x)$  are the functions of  $x$  only. These coefficients are to be determined using the boundary conditions and can be written as

$$C_1(x) = \frac{C_{ox}}{t_{Si} C_{Si}} [\phi_{s1} - (V_{GS} - V_{FB1})] \quad (3)$$

$$C_2(x) = \frac{C_{rsd}}{2t_{Si}^2 \cdot C_{Si}} [V'_{DS}] + \frac{C_{box}}{2t_{Si}^2 \cdot C_{Si}} [V'_{BG}] + \frac{C_{ox}}{2t_{Si}^2 \cdot C_{Si}} [V'_{GS}] \quad (4)$$

Now, the expression for  $\phi(x, y)$  is obtained by substituting the values of  $C_1(x)$  and  $C_2(x)$  into Eq. (2). Thus, the potential can be written as

$$\phi(x, y) = \phi_f(x) + \frac{C_{ox}}{t_{Si} \cdot C_{Si}} [\phi_f(x) - V'_{GS}] y + \left\{ \frac{C_{rsd}}{2t_{Si}^2 \cdot C_{Si}} [V'_{DS} - 2\phi_b(x)] + \frac{C_{box}}{2t_{Si}^2 \cdot C_{Si}} [V'_{BG} - \phi_b(x)] + \frac{C_{ox}}{2t_{Si}^2 \cdot C_{Si}} [\phi_f(x) - V'_{GS}] \right\} y^2 \quad (5)$$

Further, the following differential equation of front-surface potential,  $\phi_f$  has been obtained using  $\phi(x, y)$  of Eq. (2) into Eq. (1) at  $y = 0$

$$\frac{d^2\phi_f(x)}{dx^2} - \alpha_f\phi_f(x) = \beta_f \tag{6}$$

where,  $\alpha_f$  and  $\beta_f$  are

$$\alpha_f = 2 \frac{1 + \left( \frac{C_{ox}(C_{Si} + 2C_{rsd} + C_{box})}{C_{Si}(2C_{rsd} + C_{box})} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{2C_{rsd} + C_{box}} \right)} \tag{7}$$

$$\beta_f = \frac{qN_a}{\epsilon_{Si}} - V'_{GS}A_{1f} - V'_{DS}A_{2f} - V'_{BG}A_{3f} \tag{8}$$

$$A_{1f} = \frac{\left( \frac{2C_{ox}(C_{Si} + 2C_{rsd} + C_{box})}{C_{Si}(2C_{rsd} + C_{box})} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{2C_{rsd} + C_{box}} \right)}$$

$$A_{2f} = \frac{\left( \frac{2C_{rsd}}{2C_{rsd} + C_{box}} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{2C_{rsd} + C_{box}} \right)}$$

$$A_{3f} = \frac{\left( \frac{2C_{box}}{2C_{rsd} + C_{box}} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{2C_{rsd} + C_{box}} \right)} \tag{9}$$

Eq. (6) can be solved as

$$\phi_f = A_f \cdot e^{\sqrt{\alpha_f}x} + B_f \cdot e^{-\sqrt{\alpha_f}x} - \frac{\beta_f}{\alpha_f} \tag{10}$$

Now, the coefficients ( $A_f, B_f$ ) of Eq. (10) are determined using the boundary conditions as

$$A_f = \frac{\beta_f \left( e^{\sqrt{\alpha_f}L} - 1 \right) + \alpha_f \left[ V_{bi} \left( e^{\sqrt{\alpha_f}L} - 1 \right) + V_{DS} e^{\sqrt{\alpha_f}L} \right]}{\alpha_f \left( e^{2\sqrt{\alpha_f}L} - 1 \right)} \tag{11}$$

$$B_f = \frac{e^{\sqrt{\alpha_f}L} \left\{ \beta_f \left( e^{\sqrt{\alpha_f}L} - 1 \right) - \alpha_f \left[ V_{bi} \left( 1 - e^{\sqrt{\alpha_f}L} \right) + V_{DS} \right] \right\}}{\alpha_f \left( e^{2\sqrt{\alpha_f}L} - 1 \right)} \tag{12}$$

Similarly, the following differential equation of back-surface potential,  $\phi_b$  has been obtained using  $\phi(x, y)$  of Eq. (5) into Eq. (1) at  $y = t_{Si}$

$$\frac{d^2\phi_b(x)}{dx^2} - \alpha_b\phi_b(x) = \beta_b \tag{13}$$

where,  $\alpha_b$  and  $\beta_b$  are

$$\alpha_b = 2 \frac{1 + \left( \frac{(C_{ox} + C_{Si})(2C_{rsd} + C_{box})}{C_{ox}C_{Si}} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{C_{ox}} \right)} \tag{14}$$

$$\beta_b = \frac{qN_a}{\epsilon_{Si}} - V'_{GS}A_{1b} - V'_{DS}A_{2b} - V'_{BG}A_{3b} \tag{15}$$

Here

$$A_{1b} = \frac{2}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{C_{ox}} \right)}$$

$$A_{2b} = 2 \frac{\left( \frac{C_{rsd}}{C_{ox}} + \frac{C_{rsd}}{C_{Si}} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{C_{ox}} \right)}$$

$$A_{3b} = 2 \frac{\left( \frac{C_{box}}{C_{ox}} + \frac{C_{box}}{C_{Si}} \right)}{t_{Si}^2 \left( 1 + 2 \frac{C_{Si}}{C_{ox}} \right)} \tag{16}$$

Using the boundary conditions in solving Eq. (5), gives the following equation for the back-surface potential

$$\phi_b = A_b \cdot e^{\sqrt{\alpha_b}x} + B_b \cdot e^{-\sqrt{\alpha_b}x} - \frac{\beta_b}{\alpha_b} \tag{17}$$

Similarly, the coefficients  $A_b, B_b$  are determined as

$$A_b = \frac{\beta_b (e^{\sqrt{\alpha_b} L} - 1) + \alpha_b [V_{bi} (e^{\sqrt{\alpha_b} L} - 1) + V_{DS} e^{\sqrt{\alpha_b} L}]}{\alpha_b (e^{2\sqrt{\alpha_b} L} - 1)} \quad (18)$$

$$B_b = \frac{e^{\sqrt{\alpha_b} L} \left\{ \beta_b (e^{\sqrt{\alpha_b} L} - 1) - \alpha_b [V_{bi} (1 - e^{\sqrt{\alpha_b} L}) + V_{DS}] \right\}}{\alpha_b (e^{2\sqrt{\alpha_b} L} - 1)} \quad (19)$$

The minimum of the front- and back- surface potential  $\phi_{f \min, b \min}$  would determine the threshold voltage of the device. The obtained expression is

$$\phi_{f \min, b \min} = 2\sqrt{A_{f,b} B_{f,b}} - \frac{\beta_{f,b}}{\alpha_{f,b}} \quad (20)$$

### 3.1 Subthreshold Current Formulation

The subthreshold current is mainly dominated by the diffusion phenomenon and is proportional to the carrier concentration at the minimum surface potential position (virtual cathode) as calculated as

$$V_{th} = \begin{cases} V_{thf}, & \text{for } \phi_{f \min} > \phi_{b \min} \\ V_{thb}, & \text{for } \phi_{f \min} < \phi_{b \min} \end{cases}$$

Therefore, by employing the 2D surface potential function and following the methodology used in Ref. [7], the expression of subthreshold current can be written as follows:

$$I_{sub} = K \int_0^{t_{Si}} \exp\left(\frac{\phi_{vc}(y)}{V_T}\right) dy \quad (21)$$

where,  $\phi_{vc}(y)$  is the virtual cathode potential.

Now, after solving the Eq.(21), the obtained final subthreshold current expression,  $I_{sub}$  is

$$I_{sub} = KV_T \left[ \frac{I_f}{E_f} + \frac{I_b}{E_b} \right] \quad (22)$$

where,

$$I_f = \exp\left(\frac{\phi_{vc}(y=0)}{V_T}\right) - \exp\left(\frac{\phi_{vc}(y=y_m)}{V_T}\right) \quad (23)$$

$$I_b = \exp\left(\frac{\phi_{vc}(y=y_m)}{V_T}\right) - \exp\left(\frac{\phi_{vc}(y=t_{Si})}{V_T}\right) \quad (24)$$

$$E_f = (\phi_{vc}(y=0) - \phi_{vc}(y=y_m))/y_m \quad (25)$$

$$E_b = (\phi_{vc}(y=y_m) - \phi_{vc}(y=t_{Si}))/y_m \quad (26)$$

### 3.2 Subthreshold Swing Formulation

This section presents the modeling of subthreshold swing of short-channel Re-S/D SOI MOSFETs with Back-Gate Control. Sub Threshold Swing (S) of Re-S/D SOI MOSFETs with Back-Gate Control can be written as [7]

$$S = \begin{cases} \ln 10 V_T \left( 1 + \frac{C_{Si}(2C_{rsd} + C_{box})}{C_{ox}(C_{Si} + 2C_{rsd} + C_{box})} \right) \\ \left( \frac{1 + e^{\sqrt{\alpha_s} L}}{1 + e^{\sqrt{\alpha_s} L} - e^{\sqrt{\alpha_s} \phi_{f \min}} - e^{\sqrt{\alpha_s} (L - \phi_{f \min})}} \right) \text{ for } \phi_{f \min} > \phi_{b \min} \\ \ln 10 V_T \left( 1 + \frac{(C_{ox} + C_{Si})(2C_{rsd} + C_{box})}{C_{ox} C_{Si}} \right) \\ \left( \frac{1 + e^{\sqrt{\alpha_s} L}}{1 + e^{\sqrt{\alpha_s} L} - e^{\sqrt{\alpha_s} \phi_{f \min}} - e^{\sqrt{\alpha_s} (L - \phi_{b \min})}} \right) \text{ for } \phi_{b \min} > \phi_{f \min} \end{cases} \quad (27)$$

## 4. RESULTS AND DISCUSSION

In this section, we have compared the analytical results obtained from the proposed models with the numerical simulation data obtained by simulating the device structure under consideration with a commercially available 2D device simulator ATLAS<sup>TM</sup> [8].

### 4.1 Sub Threshold Current

The sub threshold current ( $I_{Sub}$ ) with the gate voltage for three different buried oxide thicknesses ( $t_{box}$ ) is plotted in Fig.2. It should be noted that the present subthreshold current model is based on only the diffusion phenomenon of current transport, and therefore, the sub threshold current can be observed in agreement with the simulation results below the threshold voltage of the device. It is observed from Fig. 2 that for the fixed values of  $V_{GS}$  the sub threshold current is decreased with the decrease in BOX thickness. This decrease of  $I_{Sub}$  using a thinner BOX may be due to larger impact of back-gate reverse bias on it. The sub

threshold current ( $I_{Sub}$ ) variation with the gate to source voltage  $V_{GS}$  for different recessed-source/drain thickness ( $t_{rsd}$ ) is considered in Fig. 3. It is found that at  $t_{rsd} = 0\text{nm}$  (conventional SOI with back-gate),  $I_{Sub}$  is  $\sim 2 \cdot 10^{-10}$  A/ $\mu\text{m}$  and as increases to 25nm, becomes  $\sim 5 \cdot 10^{-10}$  A/ $\mu\text{m}$ . It is due to the fact that a deeper recessed source/drain offers higher short-channel effects due to the stronger coupling between recessed-source/drain and channel region. Figure 4 displays the impact of different back-gate voltages over the sub threshold current variation. The sub threshold current is found to be decreased with decreasing back-gate voltage. This is because the reverse back-gate voltage decreases the front surface barrier height which, in turn, causes the inversion layer at the front-surface of the channel like conventional SOI MOSFETs.

#### 4.2 Sub Threshold Swing(S)

Figure 5 shows the variation of sub threshold swing ( $S$ ) against the device channel lengths for different BOX thicknesses. The parameter  $S$  is found to be increased with the shrinkage of channel length  $< 70\text{nm}$  resulting in the poor switching characteristics of the device. However, for a fixed gate-length, the switching characteristics are observed to be improved with decreasing values of gate oxide thickness. Since, the gate will be in better position to control the channel for smaller gate oxide thickness, the above results seem to be well justified. The impact of back-gate voltage on the subthreshold swing ( $S$ ) is presented in Fig. 6. It is observed that the reverse back-gate bias voltage can improve switching characteristics immensely. As the reverse back-gate voltage decreases from -1V to -3V the switching characteristics are found to be improved by  $\sim 30\text{mV/Dec}$  by keeping the other parameters constant.

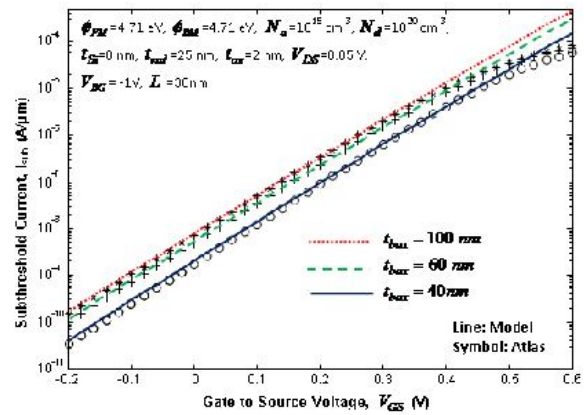


Fig.2: Sub Threshold current versus gate to source voltage for different buried oxide (BOX) thicknesses.

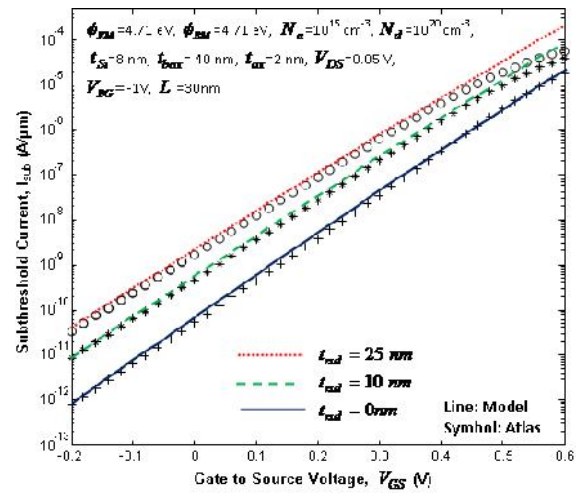


Fig.3: Sub Threshold current versus gate to source voltage for different recessed source/drain thicknesses

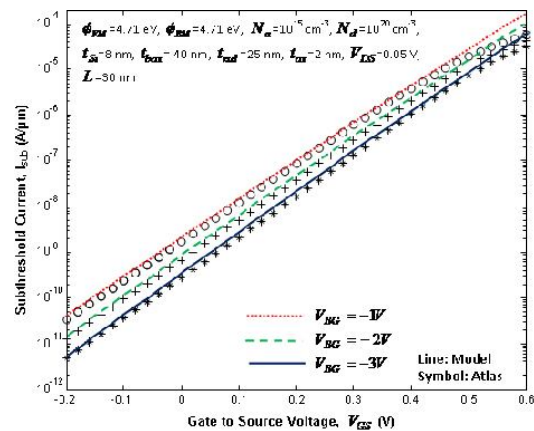
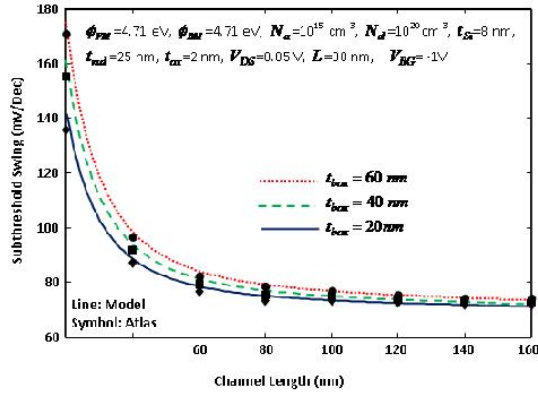
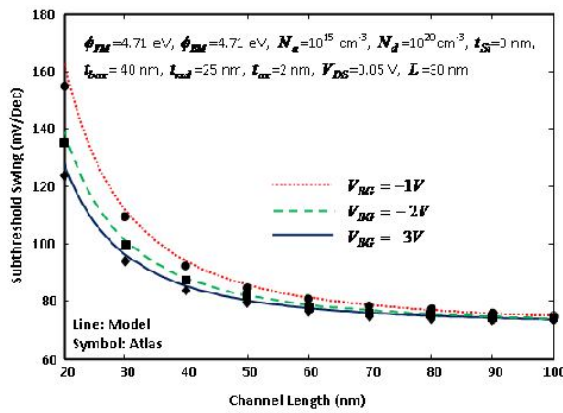


Fig.3: Sub Threshold current versus gate to source voltage for different back-gate voltage



**Fig.5:** Subthreshold swing variation with channel length for different buried oxide (BOX) thicknesses



**Fig.6:** Subthreshold swing versus channel length for different back-gate voltages

## 5. CONCLUSION

In this paper, sub threshold swing and sub threshold current models are formulated for short-channel back-gated Re-S/D SOI MOSFETs. The variations in the sub threshold current and subthreshold swing have been analyzed against the back-gate bias voltage, buried-oxide (BOX) thickness and recessed source/drain thickness. It has been found that a negative back-gate bias voltage shift the peak of inversion charge density from back-channel to the front-channel resulting in an excellent short-channel-effects immunity in the device. The sub threshold swing roll-up of the Re-S/D SOI MOSFET are found to be significantly decreased with reverse back-gate bias voltage compared to the positive or no potential at the

back-gate. Hence, the use of negative bias voltage may be a potential solution to reduce the short-channel effects in the Re-S/D SOI MOSFET. The excess short-channel effects owing to the recessed-source/drain thickness may be compensated by carefully applying the reverse back-gate bias voltage. Moreover, the model results are found to be in very good agreement with numerical simulation data obtained from ATLAS™.

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